

0017-9310(94)00137-5

# Thermal stresses and heat–mass transfer in ablating composite materials

YU. I. DIMITRIENKO

Scientific Research and Production Corporation "NPO Mashinostroeniya", Gagarina 33a, Reutov, Moscow Region 143952, Russia

#### (Received 1 February 1994)

Abstract—In designing a thermal protection made of ablating composite materials, constructors usually make calculations only for a heat field and a rate of material ablation; strength calculations are usually conducted only for determining thermoelastic stresses. However, there are known cases when thermal protection constructions designed this way and made of glass-plastics have destructed due to the action of the following effects that are usually not considered : pore pressure of gaseous pyrolise products generated in heating a composite, and shrinkage of a composite in heating up to the pyrolise temperature. To take account of these effects and conduct heat and strength calculations of thermal protection, in this paper a new mechanical—mathematical model is developed wherein ablating composites are considered to be porous multiphase media with phase transformations and chemical reactions of components in heating. The distinctive peculiarity of the model is that it allows description of the material.

## INTRODUCTION

Ablating composite materials represent the unique case when a non-stable system, that is polymer composites at high temperatures, is used premeditatively in crucial elements of construction, for example in heat protection of vehicles, in determination of a glassplastic construction resource in fire etc.

The reason for non-stability of composites lies in the fact that at high temperatures there are phase transformations, i.e. thermodestruction of polymer components with formation of a solid residue, usually a coke, and generation of a large quantity of gases in the pores.

At present, calculation methods for heat-mass transfer processes in ablating composites are well enough developed [1]: however, strength problems for their use in construction have been insufficiently studied. In the present paper the problem statement on determination of thermostresses in construction of ablating materials is given, an example of numerical solution of the problem for a cylindrical shell is presented, and peculiarities due to the presence of heat-mass transfer in the material are shown.

# MATHEMATICAL MODEL

An ablating composite material is considered to be a multiphase system consisting of four phases: the first phase is a thermo-stable filler (carbon glass fibers which are thermostable in the considered temperature interval in an inert medium); the second phase is a solid polymer binder (epoxy-phenol, phenol and other resins) which thermodestruct at high temperatures; the third phase consists of solid products of thermodestruction (usually a coke); and the fourth phase consists of gaseous thermodestruction products in pores. If strains of solid phases are considered to be small, gas filtration in the pores is assumed to be subject to Darcy's equation, and the heating process is so relatively slow that temperature equilibrium has time to reach steady state for all phases with the same temperature,  $\theta$ , then the heat-mass transfer equation system for the porous multiphase medium described is written in the following form [2, 3]:

$$\rho 2 \frac{\partial \varphi_2}{\partial t} = -J \tag{1}$$

$$\frac{\partial \rho_{g} \varphi_{g}}{\partial t} = \nabla_{x} \cdot (\mathbf{R} \mathbf{k} \cdot \nabla_{x} \rho_{g} \theta) + J \Gamma$$
(2)

 $\rho c \frac{\partial \theta}{\partial t} = \nabla_x \cdot (\hat{\underline{\lambda}} \cdot \nabla_x \theta) + \mathbf{R} c_g \varphi_g \nabla_x \theta$  $\cdot \underline{K} \cdot \nabla_x \rho_g \theta - J \Delta e^0 \quad (3)$ 

$$\nabla_x \cdot \varphi_s g - \nabla_x \varphi_g p = 0 \tag{4}$$

where  $\varphi_i$ ,  $\rho_2$  are volumetric concentrations and densities of solid phases (i = 1, 2, 3),  $\rho_g$  is the density of gas in pores,  $\varphi_g$  is porosity, g is the stress tensor of all solid phase collections, being a unified frame,  $c_i$  is the phase heat capacity, and R is the gas constant.

Volumetric coke concentration, and also porosity and concentration of a solid frame  $\varphi_s$ , can be expressed in terms of  $\varphi_2$ :

$$\varphi_3 = (\varphi_2(0) - \varphi_2)(1 - \Gamma) \frac{\rho_2}{\rho_3}$$

NOMENCLATURE			
$b_{i\kappa}$	material constants describing a change of strength and elastic features of	$\underline{\mathcal{E}}, \mathcal{E}_{ij}$	strain tensor and its components
	composites with temperature	$\theta$	temperature
$C_{\rm g}, C_i$	specific heat capacities of phases $[m^2(s^2 K^{-1})]$	$\lambda_{ij}$	components of a heat-conduction tensor $[kgm(s^3K)^{-1}]$
$D_{\mathbf{W}}$	rate of a surface ablation $[m s^{-1}]$	$v_{ii}$	Poisson coefficients
$E_i$	elasticity modules of phases	$\rho_{a}, \rho_{i}$	phase density $[kg m^{-3}]$
	$[kgm^{-1}s^{-2}]$	$\sigma_{ii}$	stress tensor's components.
$f(\mathbf{x}, t)$	shape of phase separation surface	.,	ľ
J	intensity of mass transfer from		
	polymer phase to gas $[kg(m^3 s)^{-1}]$	Subscripts	
${J}_0$	material constant characterizing a	bl	(blow) indicator of parameters of
	mass transfer from polymer phase to gas		outflowing gas into the
	$[kg (m^3 s)^{-1}]$		surroundings
$p_{\rm e}$	gas pressure on an external composite	e	(external) parameters related to the
	surface $[kg(m s^2)^{-1}]$		surroundings with respect to the
р	pore gas pressure $[kg(m s^2)^{-1}]$		considered domain
t	time [s].	g	(gas) parameters of a gas phase
		i	number of a composite phase
Greek symbols			$(i=1,\ldots,3)$
$\alpha_i, \alpha_{\kappa i}$	coefficients of heat phase expansion	i, j	indicator of a tensor component
	$[K^{-1}]$		(i, j = 1, 2, 3)
$\alpha^{T}$	coefficient of heat transfer $[kg(s^3 K)^{-1}]$	S	(solid) parameters of a solid
$\beta_{\kappa}, \beta_{ m sh}$	shrinkage coefficients		framework
Γ	gasification coefficient	V	occupied by a composite
$\Delta e^0, \Delta e^0$	e* heat of volumetric	W	parameters on an external composite
	(thermodestruction) and		surface
	surface ablation	~	indicator of a tensor.

$$\varphi_{s} = \varphi_{1} + \varphi_{2} \left( 1 - (1 - \Gamma) \frac{\rho_{2}}{\rho_{3}} \right) + \varphi_{2}(0) (1 - \Gamma) \frac{\rho_{2}}{\rho_{3}}$$
$$\varphi_{g} = 1 - \varphi_{s} \quad \varphi_{1} = \text{const.}$$
(5)

Function J describes heat-mass transfer intensity in thermodestruction in accordance with Arrhenius's law:

$$J = J_0 \varphi_2 \exp\left(-\frac{E_a}{\mathbf{R}\theta}\right). \tag{6}$$

 $\Gamma$  is the gasification coefficient of the composite in thermodestruction, and  $\lambda$  and  $\tilde{K}$  are heat-conduction and gas-permeability tensors, respectively, that depend on the porosity  $\varphi_{g}$ :

$$\underline{\lambda} = \underline{\lambda}^0 f(\varphi_g); \quad \underline{K} = \underline{K}^0 f(\varphi_g) \quad f(\varphi_g) = \exp(S\varphi_g).$$
(7)

Here  $\lambda^0$ ,  $K^0$  are constant tensors and S is the material constant.

Gas in pores is assumed to be ideal and perfect :

$$p = \mathbf{R}\rho_{\mathbf{g}}\theta \tag{8}$$

where p is pore gas pressure.

If we introduce a stress-tensor function  $\underline{F}$  so that

$$\sigma = \frac{\varphi_g}{\varphi_s} p \delta + \frac{1}{\varphi_s} \operatorname{Ink} F$$
(9)

where Ink  $\underline{F}$  is the differential operator of incompatibility [4], then equilibrium equation (4) is satisfied identically. To determine a stress-strain state in an ablating composite, the compatibility equation for strains  $\varepsilon$  [4] should be considered :

$$\operatorname{Ink} \mathfrak{E} = 0. \tag{10}$$

# Constitutive relations

The thermodestruction process of composites can be considered as a phase transformation of the polymer phase into a collection of a new solid phase and a gas phase. For media with internal phase transformations of such type, constitutive relations of their solid frame correspond to the model of viscoelastic unstable medium, even if all the phases are elastic media.

An ablating composite is assumed to be an orthotropic material with orthotropy axes  $Ox_i$ , i = 1, 2, 3, having a laminated structure, and the  $Ox_1$  axis being perpendicular to the layers.

The constitutive relations can be written in the following form:

#### **CYLINDRICAL SHELL**

Let us consider now a solution of the problem stated above for a cylindrical shell subjected both to intensive internal convective heating and internal pressure  $p_{el}$ distributed uniformly at the inner surface  $r = r_{\rm D}$ . Introduce a cylindrical coordinate system Or9z and assume the composite material of the cylinder is cylindrically orthotropic; then the constitutive relations (11)-(18) keep their validity if, in place of Descartes's components  $\sigma_{ij}$ ,  $\varepsilon_{ij}$ , their physical components, are substituted. One end of the cylinder, z = 0, is rigidly fastened and at the other end the pressure  $p_{e3}$  is given; the ends are assumed to be hermetic and heat-isolated. The exterior cylinder surface,  $r = r_2$ , is fastened together with a load-bearing shell. Due to thermomechanical ablation, the surface  $r = r_D(t)$  will be mobile.

Within the scope of these assumptions, the problem (1)–(4), (13) solution is sought in terms of functions  $\varphi_2$ ,  $\rho_g$ ,  $\theta$ ,  $F_1 \equiv F$  and  $W_1$ , depending only on r and t. Equations (9) can be rewritten in the case as follows:

$$\sigma_{11} = \frac{\varphi_{g}p}{\varphi_{s}} + \frac{F}{\varphi_{s}r} \quad \sigma_{22} = \frac{\varphi_{g}p}{\varphi_{s}} + \frac{F'}{\varphi_{s}}.$$
 (21)

The rest of the stresses are equal to zero except  $\sigma_z$ , which can be expressed by the formula

$$\sigma_{33} = \beta_{10}\sigma_{11} + \beta_{20}\sigma_{22} - p(1 - \beta_{10} - \beta_{20}) + \tilde{a}_{1}^{0}E_{3}(C - \tilde{\varepsilon}_{33}) (22)$$
$$\beta_{10} = -\frac{v_{13}\tilde{a}_{1}^{0}}{\tilde{a}_{2}} \quad \beta_{20} = -v_{23}$$

where  $C(t) = \varepsilon_{33}$  is a function of time which can be determined by the following approximate formula (when Poisson effects at the cylinder end are neglected):

$$C = \hat{\varepsilon}_{33} - \frac{p_{e3}(r_2^2 - r_1^2)}{2E_3 \int_{R_1}^{R_2} \tilde{a}_1^0 r \, \mathrm{d}r}.$$
 (23)

Here the designation  $F' \equiv \partial F / \partial r$  is introduced.

Constitutive relations (11) and (13) are reduced to the form :

$$\begin{aligned}
\varepsilon_{11} &= \dot{\tilde{\varepsilon}}_{11} + \beta_{10}C + \beta_{11}\sigma_{11} + \beta_{12}\sigma_{22} \\
\varepsilon_{22} &= \dot{\tilde{\varepsilon}}_{22} + \beta_{20}C + \beta_{12}\sigma_{11} + \beta_{22}\sigma_{22} \\
\dot{W}_{1} + \dot{\varphi}_{3}W_{1}Q_{1} &= \frac{\dot{\varphi}_{3}}{\varphi_{s}} \left(\frac{F}{r} + \varphi_{g}p\right)
\end{aligned}$$
(24)

where

$$\beta_{11} = \frac{1}{E_i \tilde{a}_1^0} - \frac{v_{3i}^2}{E_3 \tilde{a}_2^0}$$
$$\beta_{12} = -\frac{v_{12}\theta}{E_1 \tilde{a}_1^0} - \frac{v_{31}v_{32}}{E_3 \tilde{a}_2^0} \quad i = 1, 2$$
$$\tilde{\tilde{e}}_{11} = \tilde{e}_{11} + \beta_{10}(C - \tilde{e}_{33}) + W_3 p_3$$

$$\mathring{\check{\varepsilon}}_{22} = \mathring{\varepsilon}_{11} + \beta_{20}(C - \mathring{\varepsilon}_{33}) \tag{25}$$

and heat deformations  $\hat{\varepsilon}_i$ ,  $\hat{\varepsilon}_o$ ,  $\hat{\varepsilon}_z$  are expressed by formulae (15) with indexes  $\kappa = 1, 2, 3$ , respectively.

Compatibility equations (10) in this case are reduced to the one, which after substituting relations (9) and (11) into it, has the form

$$\begin{split} \bar{\beta}_{22}F'' + \left(\bar{\beta}_{22}' + \frac{\bar{\beta}_{22}}{r}\right)F' \\ + \left(\left(\frac{\bar{\beta}_{12}}{r}\right)' + \frac{\bar{\beta}_{12} - \bar{\beta}_{11}}{r}\right)F + \left(p(\bar{\beta}_{22} + \bar{\beta}_{12})\right)' \\ + \frac{\varphi_{g}p}{r}(\bar{\beta}_{22} - \bar{\beta}_{11}) + \mathring{\tilde{\varepsilon}}_{11}' + \frac{\mathring{\tilde{\varepsilon}}_{22} - \mathring{\tilde{\varepsilon}}_{11}}{r} = 0 \quad (26) \end{split}$$

where  $\bar{\beta}_{ii} = \beta_{ii}/\varphi_s$ .

 $\rho c$ 

r

Heat-mass transfer equations (1)-(3) for a cylindrical shell have the form :

$$\rho_{2}\dot{\varphi}_{2} = -J$$

$$(\rho_{g}\varphi_{g})^{\bullet} = \frac{1}{r} (\mathbf{R}K_{11}r(\rho_{g}\rho)')' + J\Gamma$$

$$\dot{\theta} = \frac{1}{r} (\lambda_{11}r\theta')' + c_{g}\mathbf{R}K_{11}\theta'(\rho_{g}\theta)' - J\Delta \mathbf{e}^{0}. \quad (27)$$

Boundary conditions for equation system (26), (27) have the form :

$$r = r_{\rm D}(t): \quad \frac{F}{r_{\rm D}} = -p_{\rm e1} \quad \mathbf{R}\rho_{\rm g}\theta = p_{\rm e1}$$
$$\dot{\lambda}_{11}\theta' = \alpha_{\rm T}(\theta_{\rm e} - \theta) - \varphi_{\rm s}\rho_{\rm s}D_{\rm W}\Delta e^{*}$$
$$-\gamma_{\rm bl}c_{\rm g}\mathbf{R}K_{11}(\rho_{\rm g}\theta)'(\theta_{\rm e} - \theta) \quad (28)$$
$$\left(F_{\rm e1}\right) \qquad E_{\rm B}h_{\rm H}$$

$$= r_{2}: \quad \varphi_{s}\left(\frac{r}{r_{2}} + \varphi_{g}p\right) = -p_{e2} - \frac{2\Gamma_{II}\pi_{II}}{(1 - v_{\Pi}^{2})r_{2}}$$

$$\times \left(\overset{\circ}{\tilde{\varepsilon}}_{22} + \bar{\beta}_{12}\left(\frac{F}{r_{2}} + \varphi_{g}p\right) + \bar{\beta}_{22}(F' + \varphi_{g}p)\right)$$

$$(\rho_{g}\theta)' = 0 \qquad (29)$$

where  $E_{\Pi}$ ,  $\nu_{\Pi}$  and  $h_{\Pi}$  are the elasticity module, the Poisson coefficient and the substrate thickness, respectively.

The equation of the inner mobile surface has the form:

$$\dot{r}_{\rm D} = D_{\rm W} \quad r_{\rm D}(0) = r_1.$$
 (30)

Introducing now a new mobile coordinate y in place of r,

$$y = k(t)r + b(t)$$

$$k(t) = \frac{r_2 - r_1}{r_2 - r_D(t)} \quad b(t) = \frac{r_2(r_1 - r_D(t))}{r_2 - r_D(t)} \quad (31)$$

varying within the interval  $r_1 \le y \le r_2$  for all  $t \ge 0$ while  $r_D(t) \le r \le r_2$ .

Introducing the auxiliary function  $\zeta(y, t)$ 

$$\zeta(\mathbf{r}, t) = \frac{D_{W}}{r_{2} - r_{D}(t)} \left( \frac{r_{2} - r_{1}}{(r_{2} - r_{D}(t))^{2}} \times \left( \frac{y - b(t)}{k(t)} + r_{2} \right) - r_{2} \right).$$
(32)

Then, passing to new variables (y, t), the equation system (26), (27) will be written in the form

$$\dot{\varphi}_2 + \zeta \varphi'_2 = -\frac{J}{\rho_2}$$
 (33)

$$\rho_{g}\varphi_{g})^{\bullet} + \zeta(\rho_{g}\varphi_{g})^{\prime}$$
$$= \frac{k^{2}}{v-b} \left( \mathbf{R}K_{11}(v-b)(\rho_{g}\theta)^{\prime} \right)^{\prime} + J\Gamma \quad (34)$$

$$\rho c \dot{\theta} + \rho c \zeta \theta' = \frac{k^2}{y - b} \left( \dot{\lambda}_{11} (y - b) \theta' \right)' + c_y k^2 \mathbf{R} K_{11} \theta' (\rho_y \theta)' - J \Delta e^0$$
(35)

$$\bar{\beta}_{22}F'' + \left(\bar{\beta}_{22}' + \frac{\bar{\beta}_{22}}{y-b}\right)F' + \left(\left(\frac{\bar{\beta}_{12}}{y-b}\right)' + \frac{\bar{\beta}_{12} - \bar{\beta}_{11}}{y-b}\right)F + \frac{1}{k}\left[\hat{\tilde{\epsilon}}_{11}' + \frac{\hat{\tilde{\epsilon}}_{22} - \hat{\tilde{\epsilon}}_{11}}{y-b} + p(\bar{\beta}_{22} + \bar{\beta}_{12})' + \frac{p}{y-b}(\bar{\beta}_{22} - \bar{\beta}_{11})\right] = 0$$
(36)

$$\dot{W}_{1} + \zeta W_{1}' + \dot{\varphi}_{3} Q_{1} W_{1} = \frac{\varphi_{3}}{\varphi_{s}} \left( \frac{T}{y - b} + \varphi_{g} p \right) \quad (37)$$

where  $F' \equiv \partial F / \partial y$ .

(

Boundary conditions (28) in variables (y, t) are written in the form

$$r = r_1$$
:  $F = -r_D p_{e1}$   $R \rho_g \theta = -p_{e1}$  (38)

$$-\lambda_{11}k\theta' = (\alpha_{\rm T} - \lambda_{\rm bl}c_{\rm g} \mathbf{R}K_{11}(\rho_{\rm g}\theta)') \times (\theta_{\rm c} - \theta) - \rho_{\rm s}\varphi_{\rm s}D_{\rm w}\Delta e^{\ast}$$
(39)

and the boundary condition (29) keeps its form. Adjoining initial conditions to the system (33)-(38), (29).

$$t = 0$$
:  $\varphi_2 = \varphi_2^0$   $\rho_g = \rho_g^0$   $\theta = \theta_0$   $W_3 = 0$ 

we get the complete problem statement to determine functions  $\varphi_2$ ,  $\rho_g$ ,  $\theta$ , F and  $W_1$ , after showing that the stresses  $\sigma_{11}$ ,  $\sigma_{22}$ ,  $\sigma_{33}$  can be evaluated according to equations (21) and (22).

## **COMPUTED RESULTS**

Solving the problem was performed numerically with the help of the step-by-step method using difference schemes and sweep procedures.

Computed results have been obtained for glassplastic on epoxy-phenol binder and silica fabric. In computations the following values of the constants were given:

$$b_{11} = 1.2 \text{ K}^{-1} (\text{s})^{b_{21}-1} \quad b_{21} = 0.42 \quad b_{31} = 5$$
  

$$b_{12} = 0.5 \text{ K}^{-1} (\text{s})^{b_{22}-1} \quad b_{22} = 0.22 \quad b_{32} = 5$$
  

$$\alpha_{21} = 20 \cdot 10^{-6} \text{ K}^{-1} \quad \alpha_{31} = 2 \cdot 10^{-6} \text{ K}^{-1} \quad \beta_{1} = 5$$
  

$$\alpha_{22} = 4 \cdot 10^{-6} \text{ K}^{-1} \quad \alpha_{32} = 2 \cdot 10^{-6} \text{ K}^{-1} \quad \beta_{2} = 0.05$$
  

$$\alpha_{23} = 4 \cdot 10^{-6} \text{ K}^{-1} \quad \alpha_{33} = 2 \cdot 10^{-6} \text{ K}^{-1} \quad \beta_{3} = 0.05$$
  

$$\rho_{1} = 2.5 \cdot 10^{3} \text{ kg m}^{-3} \quad \rho_{2} = 1.2 \cdot 10^{3} \text{ kg m}^{-3}$$
  

$$\rho_{3} = 2.2 \cdot 10^{3} \text{ kg m}^{-3} \quad c_{1} = 0.89 \text{ kJ kg}^{-1} \text{ K}^{-1},$$
  

$$c_{2} = 0.6 \text{ kJ kg}^{-1} \text{ K}^{-1} \quad c_{3} = 1.5 \text{ kJ kg}^{-1} \text{ K}^{-1}$$
  

$$c_{g} = 3.1 \text{ kJ kg}^{-1} \text{ K}^{-1} \quad \lambda_{13} = 0.51 \text{ W tm}^{-3} \text{ K}^{-1}$$
  

$$\lambda_{23} = 0.27 \text{ W tm}^{-3} \text{ K}^{-1} \quad \lambda_{33} = 0.5 \text{ W tm}^{-3} \text{ K}^{-1}$$
  

$$\lambda_{g3} = 0.1 \text{ W tm}^{-3} \text{ K}^{-1} \quad J_{0} = 3.2 \cdot 10^{6} \text{ kg m}^{-3} \text{ s}^{-1}$$
  

$$E_{a}/\text{R} = 5.5 \cdot 10^{3} \text{ K} \quad \Gamma = 0.78$$
  

$$K^{0} = 1.8 \cdot 10^{-19} \text{ s} \quad S = 100 \quad \sigma_{b} = 200 \text{ MPa}$$
  

$$n = 5 \quad E_{1} = 20 \text{ GPa} \quad E_{2} = 20 \text{ GPa}$$
  

$$E_{3} = 2 \text{ GPa} \quad v_{12} = 0.27 \quad v_{23} = 0.021$$
  

$$v_{13} = 0.021 \quad G_{12} = 8 \text{ GPa}$$
  

$$G_{23} = 0.72 \text{ GPa} \quad G_{13} = 0.72 \text{ GPa}.$$

Geometric parameters and characteristics of the load-bearing shell were chosen as follows:

$$r_1/r_2 = 0.97$$
  $h_{\Pi} = 2 \cdot 10^{-3} \text{ m}$   
 $v_{\Pi} = 0.3$   $E_{\Pi} = 6 \cdot 10^4 \text{ MPa.}$ 

Conditions of thermo-force loading the cylinder are shown in Fig. 1: for time t = 0.2 s the temperature  $\theta_e$ and the pressure  $p_e$  of gas flowing along the inside



Fig. 1. Dependence of temperature  $\theta_e$  and pressure  $p_{e1}$  of external gas medium, temperature  $\theta_w$  of the cylinder surface heated and relative thickness  $\Delta r$  of material, moved away in time, where t is time [s].



Fig. 2. Distribution of temperature  $\theta$  and pore pressure p vs the cylinder thickness, taking account of surface ablation. Symbols on curves are time t [s].



Fig. 3. Distribution of volumetric phase concentrations  $\varphi_2$ ,  $\varphi_3$  and coefficient of change of elastic properties  $\vec{a}_1^0$  vs the ablating cylinder thickness for different times. Symbols on curves are time t [s].

of the cylinder rapidly reach a stationary state. In a stationary interval of heating, the material surface temperature  $\theta_w$  slowly increases, and simultaneously the composite surface ablation occurs practically by linear law [see Fig. 1, the curve  $\Delta r(t)$ , where  $\Delta r = (r_D(t) - r_1)/r_2$ ].

Due to the presence of a surface ablation, there exists a solution only in the interval  $\bar{r}_{\rm D}(t) \leq \bar{r} \leq 1$ ; therefore on the left from the point  $r = r_{\rm D}(t)$  all the functions terminate (Figs. 2–5).

As seen from Fig. 2, the pore pressure p is localized in a comparatively narrow zone corresponding to the interval where the temperature falls off. It is connected to the fact that, in a colder zone where the composite is not heated to thermodestruction temperatures, the material gas-permeability is very small, but in a zone coked, with porosity  $\varphi_g \approx 0.26$ , on the contrary, great rates of gas filtration to the internal surface arise, leading to equalization of p with the inner pressure  $p_{el}$ .

In the computations the value of the initial material porosity was varied,  $\varphi_g^0 = 0.05$  and 0.1. A considerable value of the inner pressure  $p_{el}$ , which is characteristic for problems of this type, leads to an increase in the compressing radial stress  $\sigma_r$  (Fig. 4), having at initial time t < 3 s practically a linear distribution through the thickness. Peaks of stresses  $\sigma_r$  which appear when t > 3 s are connected to a local growth of pore pressure p in a composite thermodestruction zone. For a material with initial porosity  $\varphi_g = 0.05$ , the value of these peaks is substantially more than for  $\varphi_g = 0.1$ , and when t > 12 s, local tensile stresses arise in the composite.

A profile of the stress  $\sigma_9$  at initial time  $t \leq 10$  s is



Fig. 4. Distribution of radial stress  $\sigma_r$  vs the ablating cylinder thickness. Symbols on curves are time t [s].



Fig. 5. Distribution of tangential stress  $\sigma_{\theta}$  vs the ablating cylinder thickness for different times. Symbols on curves are time t [s].

determined, in the main, by the presence of the inner gas pressure  $p_{e1}$  and by the temperature gradient. That is why there are tensile stresses through all the cylinder thickness and a minimum of  $\sigma_{\vartheta}$  at the internal surface (Fig. 5). When  $t \ge 10$  s, a material thermodestruction becomes essential, leading to an increase in two additional factors having an effect on the stress  $\sigma_{\vartheta}$ , a formation of local pore pressure and a composite shrinkage in coking. The local pore pressure causes local minimums of  $\sigma_{\vartheta}$  to appear, but the shrinkage, on the contrary, leads to increasing the stresses  $\sigma_{\vartheta}$  at the internal cylinder surface. Decreasing the glass-plastic thickness practically to half-thickness due to surface ablation leads to an increase in the maximum of stresses  $\sigma_{\vartheta}$  from 60 to 85 MPa.

As follows from Fig. 5, it is tangential stresses  $\sigma_{s}$  that are the most dangerous for similar types of glassplastic constructions that are connected to the presence of the high inner pressure  $p_{el}$ , displacing the stress  $\sigma_r$  into the domain of negative values.

# CONCLUSIONS

The problem statement, to determine thermostresses in constructions made of ablating composite materials, is given. Evaluation of these stresses is very important in high temperature techniques, for example in designing thermal protection for spacecraft, ignition chambers for solid fuel engines, or construction resources made from composites for use in fires, etc. The example of numerical solution of the problem for non-stationary heating of a cylindrical shell shows that thermostresses have peculiarities for ablating composites that connect with internal gas generation in material and chemical shrinkage in coking.

### REFERENCES

- 1. Yu. V. Polejaev and F. B. Yurevich, *Thermal Protection*. Energy (1976) (in Russian).
- Yu. I. Dimitrienko and I. S. Epifanovskii, Deforming and strength of destructing thermal protective materials at high temperatures. *Mech. Compos. Mater.* No. 3, 460– 468 (1990) (in Russian).
- 3. Yu. I. Dimitrienko, Destruction of composite materials at high temperatures and finite strains. *Mech. Compos. Mater.* No. 1, 43-55 (1992) (in Russian).
- 4. B. E. Pobedrya, *Lectures on Tensor Analysis*. Izd-vo MSU (1986) (in Russian).